Fiscal & Financial System in Japan A 2010 Spring <u>Session 9</u> <u>The Term Structure of Interest Rates</u>

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6. The Term Structure of Interest Rats (Mishkin Ch.6)

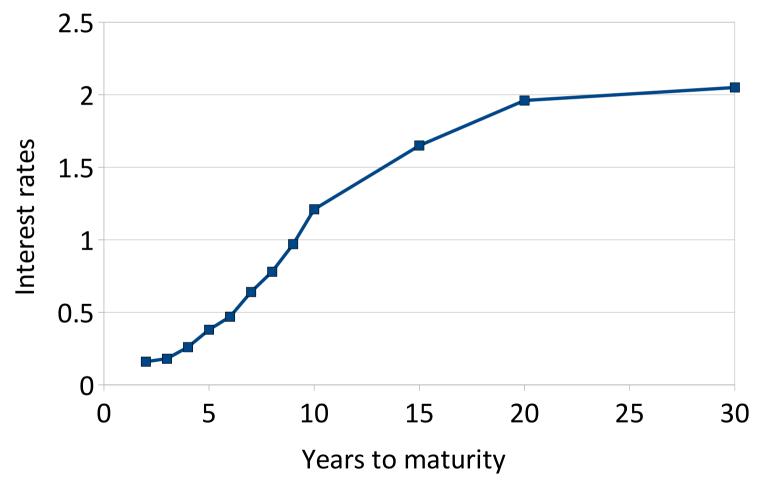
Interest rates on Japanese government bonds (as of June 9, 2010)

Years to maturity	Maturity date	Interest rate
2	06/15/2012	0.16
3	03/20/2013	0.18
4	03/20/2014	0.26
5	03/20/2015	0.38
6	03/20/2016	0.47
7	06/20/2017	0.64
8	03/20/2018	0.78
9	03/20/2019	0.97
10	06/20/2020	1.21
15	03/20/2025	1.65
20	03/20/2030	1.96
30	03/20/2040	2.05

Source: Bloomberg.co.jp(http://www.bloomberg.co.jp/index.html)

Yield Curve

Yield Curve ... Plot of yields on bonds with different maturities, but the same risk and liquidity

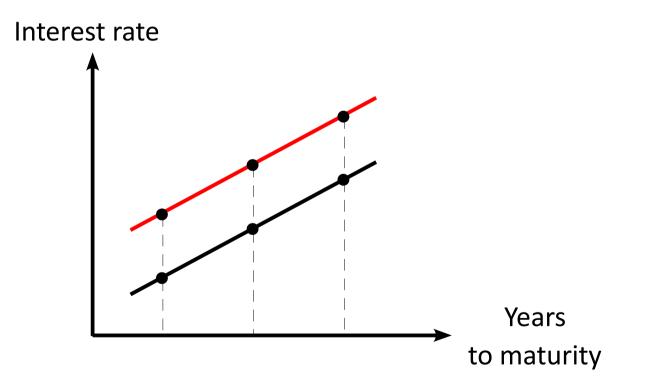


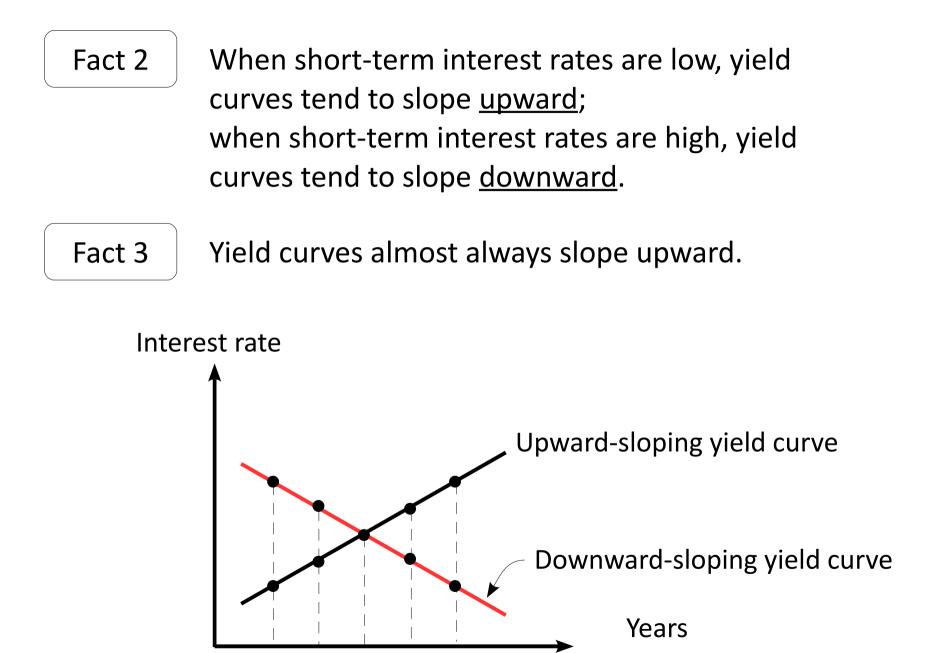
Example: Yield curve for Japanese government bonds

Three Empirical Facts on Yield Curves

Fact 1

Interest rates on bonds with different maturities move together over time.





to maturity

Term Structure and Economic Theory

Find a theory that explains all of the "three empirical facts" consistently.

Economists have developed three theories.

- Expectations theory
 Segmented markets theory
 Liquidity premium theory

Expectations Theory

Theory or Model is a set of assumptions on the behavior of people.

Assumption 1. Perfect substitutes

For investors, bonds with different maturities are *perfect substitutes*.

Investors do not prefer one maturity to another, if the other conditions are equal.

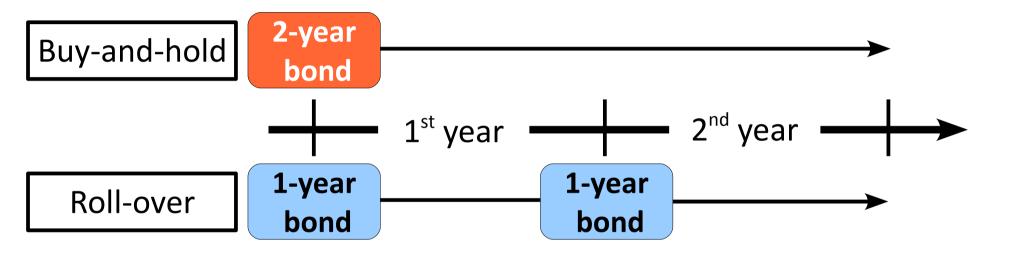
Assumption 2. Risk-neutrality

Investors are *risk-neutral*.

Investors care only about the *expected* yields, whatever the variability is.

Assumption 1: Perfect Substitutes

Suppose you invest your money for two years.



The theory *assumes* that ...

for investors, the two strategies are equivalent, and thus perfectly substitutable.

Assumption 2: Risk-neutrality

Investment 1. 7% yield with certainty

Investment 2. 10% yield with the prob of 0.7, and no yield with 0.3

 $10\% \times 0.7 + 0\% \times 0.3 = 7\%$

7% yield on average

Expected Yield

The theory also assumes that ...

for investors, the two investments are equivalent, or investors <u>care only about the expected yields and</u> <u>never care about volatilities or *risks*. Risk-neutral</u>

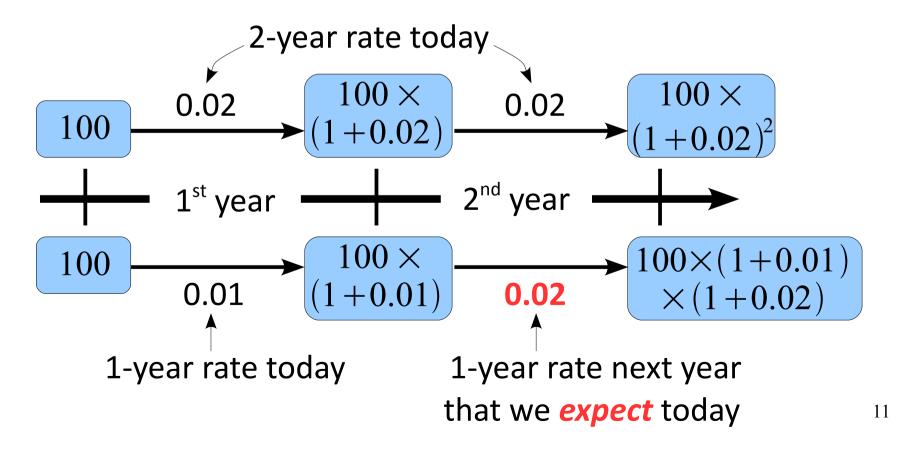
Implication of the Theory

Suppose that

(1) the yield on 2-year bond today is 0.02,

(2) the yield on 1-year bond today is 0.01, and

(3) the yield on 1-year bond next year is *expected to be* 0.02



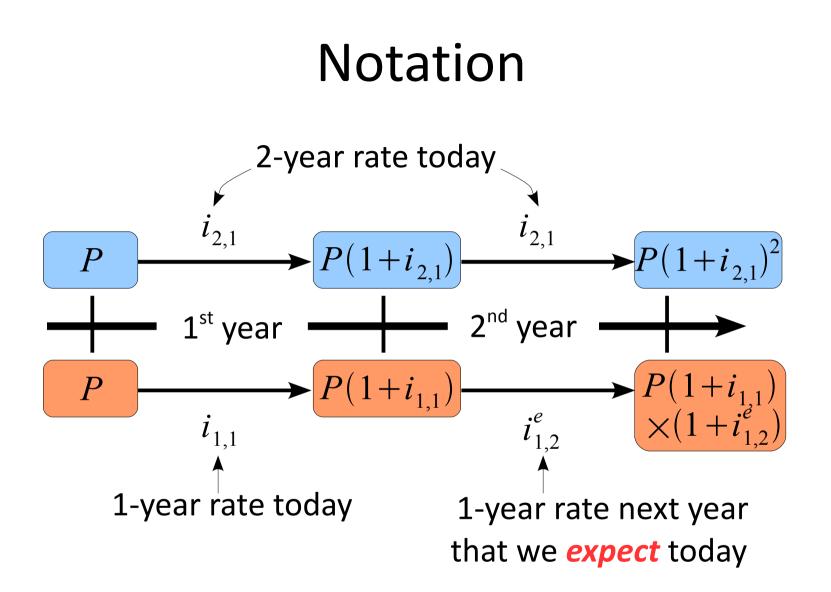
<u>Perfect substitutability</u> and <u>risk-neutrality</u> implies...

- If yield on buy-and-hold > (expected) yield on roll-over
- → Everyone tries to replace 1-year bond with 2-year bond.
- → Rise in 2-year bond price, fall in 1-year bond price today
- → Fall in 2-year yield, rise in 1-year yield today

The process continues until

yield on buy-and-hold = (expected) yield on roll-over

This specifies the relationship among the yields on 1-yearand 2-year bonds.The term structure ofinterest rates12



Buy-and-hold Roll-over

$$P(1+i_{2,1})^{2} = P(1+i_{1,1})(1+i_{1,2}^{e})$$

$$1+2i_{2,1}+(i_{2,1})^{2} = 1+i_{1,1}+i_{1,2}^{e}+i_{1,1}i_{1,2}^{e}$$
Very small and negligible

$$2i_{2,1} = i_{1,1}+i_{1,2}^{e}$$

$$i_{2,1} = \frac{i_{1,1}+i_{1,2}^{e}}{2}$$

The yield on 2-year bond today equals

the average of $\left\{ egin{array}{ll} (1) \mbox{ the yield on 1-year bond today} \\ (2) \mbox{ the expected yield on 1-year bond next year} \end{array}
ight.$

$$i_{1,1} \quad i_{1,2}^{e} \quad i_{1,3}^{e} \quad i_{1,n}^{e}$$

$$+ 1^{\text{st}} \text{ year } + 2^{\text{nd}} \text{ year } + 3^{\text{rd}} \text{ year } + 2 \xrightarrow{\text{rd}} n^{\text{th}} \text{ year } + 2 \xrightarrow{\text{rd}} n^{\text{rd}} \xrightarrow{\text{rd}} n^{\text{rd}} + 2 \xrightarrow{\text{rd}} n^{\text{rd}} \xrightarrow{\text{rd}} \xrightarrow{\text{rd}} n^{\text{rd}} \xrightarrow{\text{rd}} \xrightarrow{\text{rd}} \xrightarrow{\text{rd}} n^{\text{rd}} \xrightarrow{\text{rd}} \xrightarrow$$

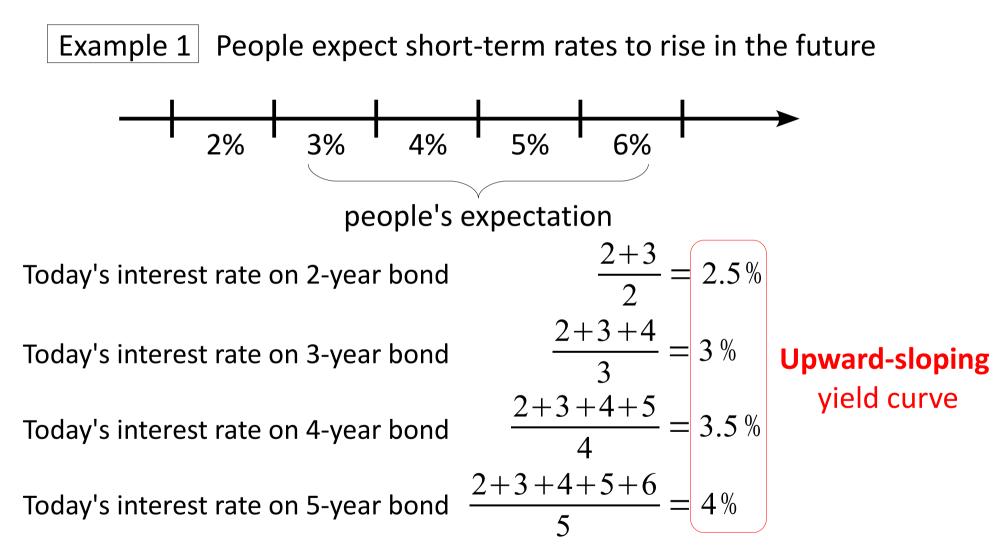
The yield on n-year bond today equals

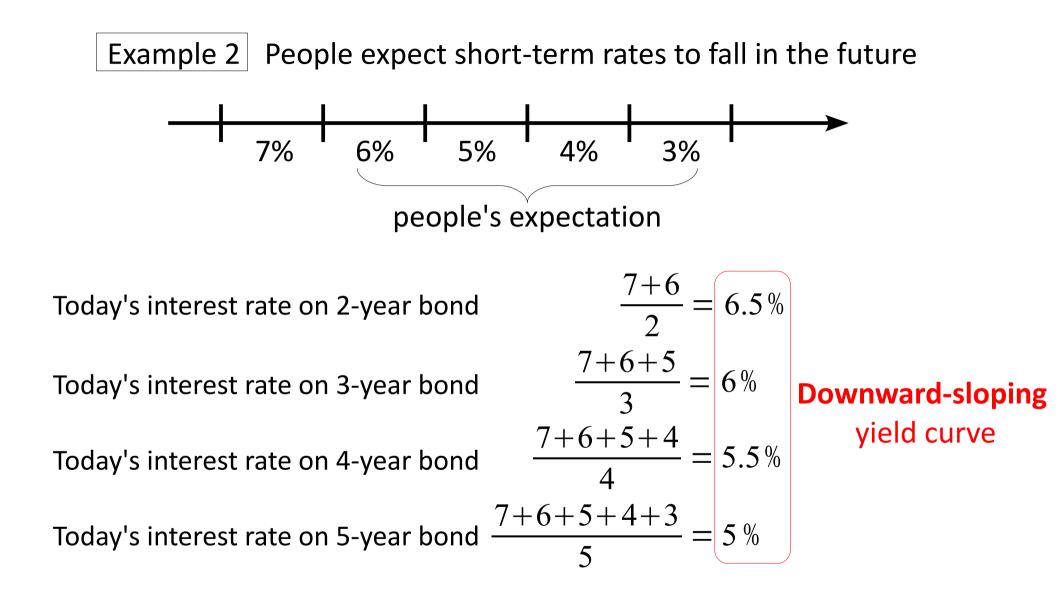
The theory implies that

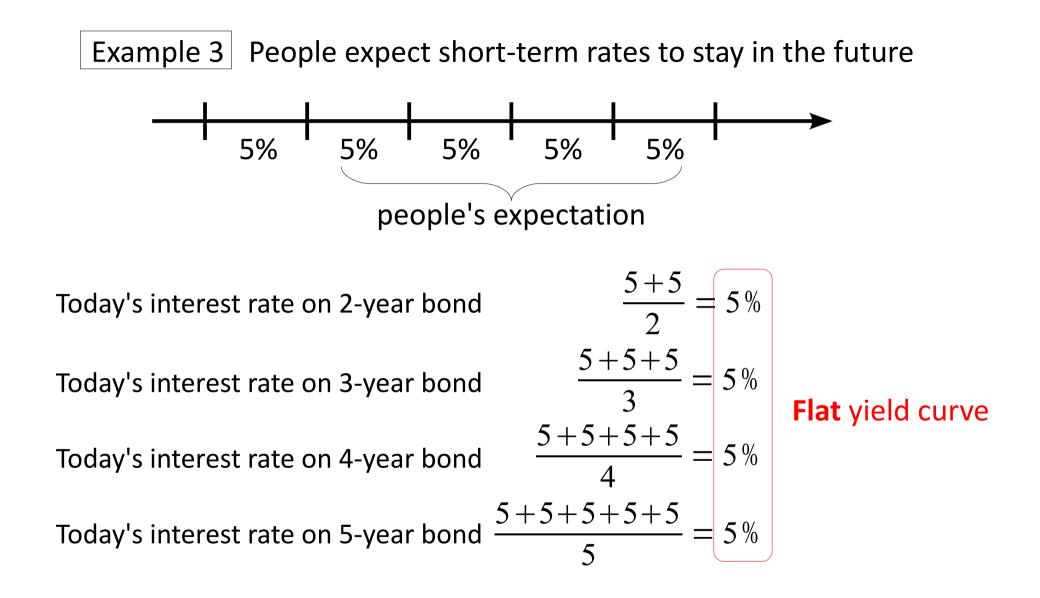
the yields on longer maturities depend on people's **expectations** of 1-year yields in the future.

Expectations Theory

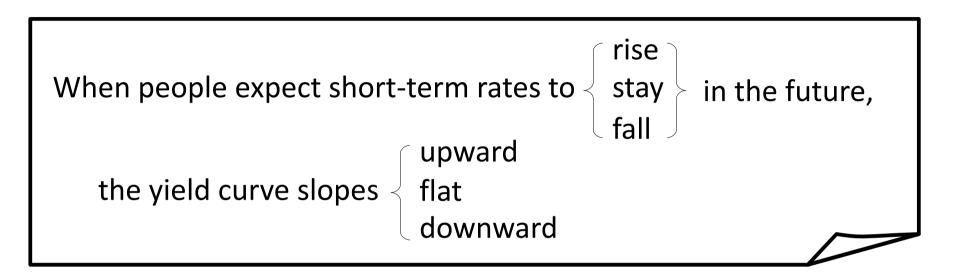
Numerical Examples

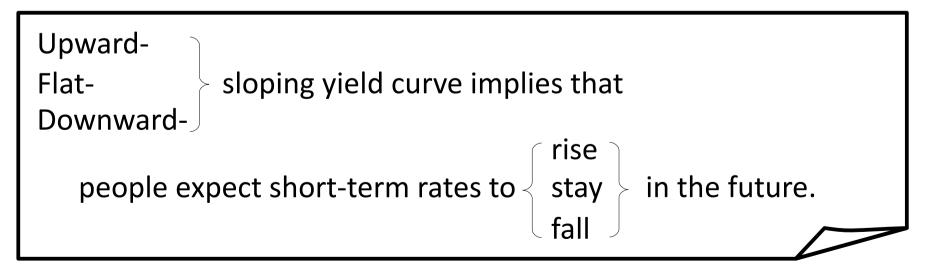






Expectation \Leftrightarrow Yield Curves





Expectation Theory and Fact 2

When a short-term rate today is relatively low ...

- → It is more likely to rise (or return to some *normal level*).
- → People expect short-term rates to rise in the future.
- → Expectations theory predicts <u>upward</u>-sloping yield curve.

When a short-term rate today is relatively high ...

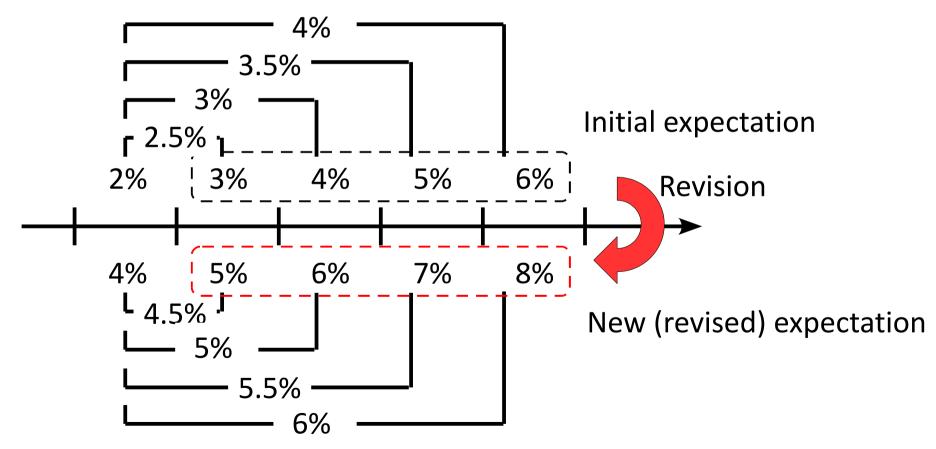
- → It is more likely to fall (or return to some *normal level*).
- → People expect short-term rates to fall in the future.
- → Expectations theory predicts <u>downward</u>-sloping yield curve.

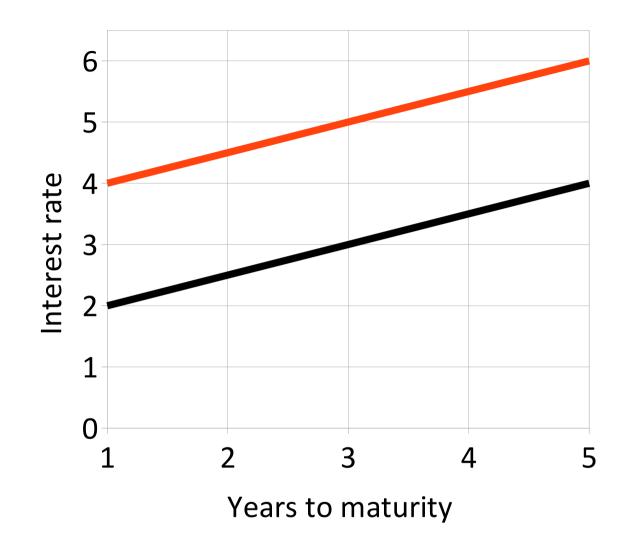
Predictions by expectations theory are consistent with "Fact 2."

Expectation Theory and Fact 1

Suppose that the central bank raises a short-term rate today. People interpret the action as a change in monetary policy

and <u>revise</u> their expectations on the future short-term rates upward.





Predictions by expectations theory are consistent with "Fact 1."